

# Sitzung 7: Zufall

Reenactment Historischer Computer  
(Sommersemester 2022)

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# Today

- ① Real randomness
- ② Pseudo randomness in computers
- ③ Randomness by Lutz on a Z22

## Motivation: Why do Computers Need Random Numbers?

- ▶ Cryptography: Generate numbers that cannot be predicted
- ▶ Statistics: Select  $n\%$  of the items
  - ▶ Without pre-determining which ones!
- ▶ Video games: Make enemy behaviour less predictable
- ▶ ...

## Sources for Real Randomness

- ▶ Some physical phenomena show some random behaviour
  - ▶ Atmospheric noise, based on lightning strikes in the atmosphere (ca. 40 lightning flashes per second)
    - ▶ We cannot predict when and where exactly a lightning strikes
  - ▶ Radioactive decay
    - ▶ Iodine-123 halves its mass in 13 hours, but we don't know which atom decays when
  - ▶ Mouse movement in a computer
    - ▶ Less random, because some areas are used more frequently than others
  - ▶ Throwing dice
    - ▶ Mostly random, but assumptions apply

## Real Randomness in a Computer

`https://www.random.org/`

- ▶ Randomness via atmospheric noise
- ▶ Distributed radios pick up noise
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# Real Randomness in a Computer

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- ▶ Randomness via atmospheric noise
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- ▶ Could someone affect the numbers by broadcasting a radio signal?
  - ▶ Theoretically, yes. Practically, no.
- ▶ Why is there a limit to the amount of randomness I can use per day?
  - ▶ Generating true random numbers takes time
  - ▶ Each radio: ca.  $12\,000 \frac{\text{bit}}{\text{s}}$
  - ▶ If all bits are used, one has to wait


www.amazon.de/TrueRNG-V3-Hardware-Random-Gen

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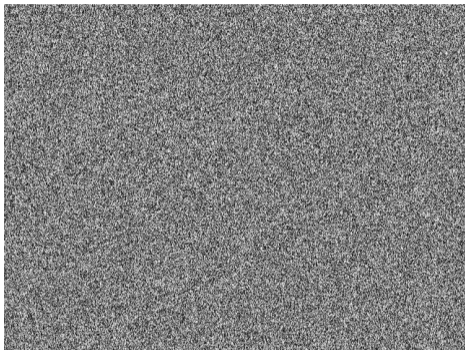


# TrueRNG

- ▶ <https://ubld.it/products/truerng-hardware-random-number-generator/>
- ▶ Source of randomness: Avalanche effect in a semiconductor junction
  - ▶ “Avalanche noise is caused by the behavior of electrons in a reverse biased diode”
- ▶ Read speed:  $400 \frac{\text{kbit}}{\text{s}}$

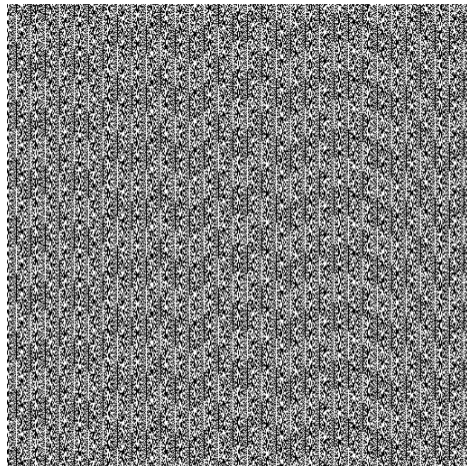
Lampert et al. (2016, 2)

# TrueRNG



true randomness from random.org

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php's rand() function

16, 2)

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  - ▶ Memory allocation
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```
653159
267853
777820
375951
833820
723985
988230
882388
775839
683704
```



# Lutz' Pseudo Random Numbers Generator

1700 B5  
1701 T1712  
1702 B1713  
1703 LLA0  
1704 LLA0  
1705 A1713  
1706 RA0  
1707 RA0  
1708 RA0  
1709 RA0  
1710 U1713  
1711 CI15  
1712 0  
1713 12345678 '  
  
1720 F1700  
1721 U14

E 1720E

# Lutz' Pseudo Random Numbers Generator

	<i>a</i>	<i>b</i>	<i>c</i>	5
1700 B5				
1701 T1712				
1702 B1713	0	E1700		E1721
1703 LLA0	1	B5	E1701	
1704 LLA0	2	E1721	E1701	
1705 A1713	3	E1721	T1712	E1702
1706 RA0	4	0	E1702	
1707 RA0	5	0	B1713	E1703
1708 RA0	6	12345678	E1702	
1709 RA0	7	"	LLA0	E1704
1710 U1713	8	45382712	E1704	
1711 CI15	9	"	LLA0	E1705
1712 0  E1721	10	157520848	E1705	
1713 12345678'	11	"	A1713	E1706
1720 F1700	12	205 876 576	E1706	
1721 U14	13	---		
	14	13117282	E1710	
	15	"	U1713	E1711

# Lutz' Pseudo Random Numbers Generator

	<i>a</i>	<i>b</i>	<i>c</i>	5
1700 B5				
1701 T1712				
1702 B1713	15 <del>AB117282</del>	<del>E1700</del>	<del>E1721</del>	
1703 LLA0	16 13 117282	U1713	E1711	
1704 LLA0	17 "	E1711		
1705 A1713	18 "	CI15	E1712	
1706 RA0	19 2	E1712		
1707 RA0	20 2	E1721		
1708 RA0				
1709 RA0	21	U14	E1722	
1710 U1713	22			
1711 CI15	23			
1712 0   E1721	24			
1713 <del>12345678</del> 13 117282	25			
1720 F1700	26			
1721 U14	27			
	28			
	29			
	30			

		<i>a</i>	<i>b</i>	<i>c</i>	5	1712
1700	B5					
1701	T1712	1	E1700		E1721	0
1702	B1713	2	B5	E1701	E1721	0
1703	LLA0	3	E1721	E1701	E1721	0
1704	LLA0	4	E1721	T1712	E1721	0
1705	A1713	5	0	E1702	E1721	E1721
1706	RA0	6	0	B1713	E1703	E1721
1707	RA0	7	12345678	E1703	E1721	E1721
1708	RA0	8	12345678	LLA0	E1704	E1721
1709	RA0	9	49382712	E1704	E1721	E1721
1710	U1713	10	49382712	LLA0	E1705	E1721
1711	CI15	11	197530848	E1705		E1721
1712	0	12	197530848	A1713	E1706	E1721
1713	12345678	13	209876526	E1706		E1721
		14	209876526	RA0	E1707	E1721
		15	104938263	E1707		E1721
1720	F1700	16	104938263	RA0	E1708	E1721
1721	U14	17	52469131	E1708		E1721
		18	52469131	RA0	E1709	E1721
		19	26234565	E1709		E1721
		20	26234565	RA0	E1710	E1721
		21	13117282	E1710		E1721
		22	13117282	U1713	E1711	E1721
		23	13117282	E1711		E1721
		24	13117282	CI15	E1712	E1721
		25	2	E1712		E1721
		26	2	E1721	E1713	E1721

## Randomness in Lutz' Program

$$\begin{aligned}x_0 &= 12345678 \\x_{n+1} &= (x_n \ll 4) + x_n \gg 4 \\ &= (16x_n + x_n) \gg 4 \\r_n &= x_{n+1} \wedge \text{16} \text{ 15}\end{aligned}$$

```
1 class LutzRandom:
2     def __init__(self):
3         self.x = 12345678
4
5     def nextnumber(self):
6         x1 = ((self.x << 4) + self.x) >> 4
7         self.x = x1 & (2**38-1)
8         return (x1 & 15)
```

- ▶ Simple algorithm to generate pseudo random numbers
- ▶ Internal value increases continuously – 38bit overflow quickly
  - ▶ First overflow after 200 numbers

# Randomness in Lutz' Program

## Evaluation

