## Recap

- Types and tokens
- Zipf distribution
- Type-Token-Ratio
- Encoding
- Unicode
- Concordances


## Collocations

# Sprachverarbeitung (VL + Ü) 

Nils Reiter

April 20, 2023

## Unicode

Much wow, DHL.
Versandmarken bei einem weltweiten Logistiker kaufen, der seine IT voll unter Kontrolle hat.


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```

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        3
    Section 1

Basic Probability Theory

## Example：Cards


－ 32 cards $\Omega$（sample space）
－ 4 icolors：$C=\{\boldsymbol{\phi}, \boldsymbol{巾}, \diamond, \bigcirc\}$
－ 8 values：$V=\{7,8,9,10, J, Q, K, A\}$
－Individual cards（っoutcomesヶ）are denoted with value and color： 8 O

## Basics

## Events

- Generally, we draw cards from a (well shuffled) deck
- We define what events we are interested in
- An event can be any subset of the sample space $\Omega$
- Events will be denoted with $E$


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- $»$ We draw card with a diamond« $-E=\{7 \diamond, 8 \diamond, 9 \diamond, 10 \diamond, J \diamond, Q \diamond, K \diamond, A \diamond\}$
- "We draw a queen «- $E=\{Q \&, Q \boldsymbol{\wedge}, Q \diamond, Q \odot\}$
- „We draw a heart eight or diamond 10 «


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- "We draw a queen « $-E=\{Q \mathbf{\&}, Q \boldsymbol{\wedge}, Q \diamond, Q \odot\}$
- »We draw a heart eight or diamond $10 «-E=\{80,10 \diamond\}$
- „We draw any card"


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- WWe draw a queen « - $E=\{Q \boldsymbol{\&}, Q \boldsymbol{\uparrow}, Q \diamond, Q \bigcirc\}$
- »We draw a heart eight or diamond $10 «-E=\{8 \circlearrowright, 10 \diamond\}$
- »We draw any card«-E= $\Omega$


## Basics

## Probabilities

- Probability $p(E)$ : Ratio of size of $E$ to size of $\Omega$ (Laplace)
- $0 \leq p \leq 1$
- $p(E)=0$ : Impossible event $\quad p(E)=1$ : Certain event
- $p(E)=0.000001$ : Very unlikely event


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## Example

- If all outcomes are equally likely: $p(E)=\frac{|E|}{|\Omega|}$
- $p(\{80\})=\frac{1}{32}$
- $p(\{9 \downarrow, 9 \downarrow, 9 \diamond, 9 \odot\})=\frac{4}{32}$
- $p(\Omega)=1$ (must happen, certain event)


## Basics

Probability and Relative Frequency

- Probability $p$ : Theoretical concept, idealization, expectation
- Relative Frequency $f$ : Concrete measure
- Normalised number of observed events


## Example

After 10 cards (with returning and shuffling), the event took place 8 times: $f(\{\boldsymbol{\omega}\})=\frac{8}{10}$

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- For large numbers of drawings, relative frequency approximates the probability
- $\lim _{\infty} f=p$
- In practice, we will often use determine probabilities by counting relative frequencies
- Assumption: Frequency is measured on representative and large data set


## Independent Events

## Joint Probability

- We are often interested in multiple events (and their relation)
- $E$ : We draw 80 two times in a row (putting the first card back)
- $E_{1}$ : First card is 80
- $E_{2}$ : Second card is 80
- $p(E)=p\left(E_{1}, E_{2}\right)=p\left(E_{1}\right) * p\left(E_{2}\right)=\frac{1}{32} * \frac{1}{32}=0.0156$


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- $E$ : We draw $\triangle$ two times in a row (putting the first card back)
- $E_{1}$ : First card is $X \odot$
- $E_{2}$ : Second card is $X \bigcirc$
- $p(E)=p\left(E_{1}, E_{2}\right)=p\left(E_{1}\right) * p\left(E_{2}\right)=\frac{1}{4} * \frac{1}{4}=0.0625$


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- These events are independent
- because we return and re-shuffle the cards all the time
- Drawing 80 the first time has no influence on the second drawing
- Default case with dice


## Dependent Events

Conditional Probability

- We no longer return the card
- E: We draw $8 \bigcirc$ two times in a row
- $E_{1}$ : First card is 80
- $E_{2}$ : Second card is 80
- $p\left(E_{1}, E_{2}\right)=p\left(E_{1}\right) * p\left(E_{2}\right)$
- This no longer works, because the events are not independent
- Obvious: Only one 80 in the game, and $p\left(E_{2}\right)$ has to express that it might be gone


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- This no longer works, because the events are not independent
- Obvious: Only one 80 in the game, and $p\left(E_{2}\right)$ has to express that it might be gone
- This is done with the notion of conditional probability
- $p\left(E_{1}, E_{2}\right)=p\left(E_{1}\right) * p\left(E_{2} \mid E_{1}\right)$
- $p\left(E_{2} \mid E_{1}\right)=0$, therefore $p(E)=0$


## Dependent Events

Conditional Probability
A less obvious example:

- We draw two cards in a row
- $E_{\varrho}$ : Card is $X \bigcirc$
- $E_{\diamond}:$ Card is $X \diamond$


## Dependent Events

Conditional Probability
A less obvious example:

- We draw two cards in a row
- $E_{\circlearrowleft}$ : Card is $X \bigcirc$
- $E_{\diamond}:$ Card is $X \diamond$

$$
\begin{aligned}
p\left(E_{\circlearrowleft}, E_{\circlearrowleft}\right) & =p\left(E_{\circlearrowleft}\right) * p\left(E_{\circlearrowleft} \mid E_{\circlearrowleft}\right) \\
& =
\end{aligned}
$$

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A less obvious example:

- We draw two cards in a row
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$$
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p\left(E_{\circlearrowleft}, E_{\circlearrowleft}\right) & =p\left(E_{\circlearrowleft}\right) * p\left(E_{\circlearrowleft} \mid E_{\circlearrowleft}\right) \\
& =\frac{8}{32} *
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$$
\begin{aligned}
p\left(E_{\bigcirc}, E_{\circlearrowleft}\right) & =p\left(E_{\bigcirc}\right) * p\left(E_{\circlearrowleft} \mid E_{\circlearrowleft}\right) \\
& =\frac{8}{32} * \frac{7}{31}=0.056
\end{aligned}
$$

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& =\frac{8}{32} * \frac{7}{31}=0.056 \\
p\left(E_{\diamond}, E_{\circlearrowleft}\right) & =p\left(E_{\diamond}\right) * p\left(E_{\circlearrowleft} \mid E_{\diamond}\right) \\
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A less obvious example:

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p\left(E_{\bigcirc}, E_{\bigcirc}\right) & =p\left(E_{\bigcirc}\right) * p\left(E_{\bigcirc} \mid E_{\bigcirc}\right) \\
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p\left(E_{\diamond}, E_{\bigcirc}\right) & =p\left(E_{\diamond}\right) * p\left(E_{\bigcirc} \mid E_{\diamond}\right) \\
& =\frac{8}{32} * \frac{8}{31}=0.064
\end{aligned}
$$

## Conditional and Joint Probabilities

Another Example

- Setup: We make a survey in a street in Cologne
- We count four types of events in two random variables:
- Person has brown hair $(H=B)$
- Person has red hair $(H=R)$
- Person likes to wake up late ( $W=L$ )
- Person likes to wake up early ( $W=E$ )


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- Person has brown hair $(H=B)$
- Person has red hair $(H=R)$
- Person likes to wake up late ( $W=L$ )
- Person likes to wake up early ( $W=E$ )
- Assumption: $B / R$ and $L / E$ are mutually exclusive
- I.e., a single person cannot have red and brown hair
- A single person can be encoded with two symbols (e.g., »BL«)

A But this combination is not unique - in contrast to the cards example

- All following numbers are made up


## Conditional and Joint Probabilities

Example

Relation between hair color $H$ and preferred wake-up time $W$

| $\downarrow W / H \rightarrow$ | brown | red | sum |
| :--- | ---: | ---: | ---: |
| early | 20 | 10 | 30 |
| late | 30 | 5 | 35 |
| sum | 50 | 15 | 65 |

Table: Survey Results, $\Omega$ : Group of questioned people

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If we pick a random person, what's the probability that this person has brown hair?

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p(H=\text { brown })=
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$$
\left.\begin{array}{l}
p(H=\text { brown })=\frac{50}{65} \quad p(H=\text { red })=\frac{15}{65} \\
p(W=\text { early })=\frac{30}{65} \quad p(W=\text { late })=\frac{35}{65}
\end{array}\right\} \text { sums per row or column }
$$

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- Joint probability: $p(W=$ late, $H=$ brown $)=\frac{30}{65}$
- Probability that someone has brown hair and prefers to wake up late
- Denominator: Number of all items


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- Joint probability: $p(W=$ late, $H=$ brown $)=\frac{30}{65}$
- Probability that someone has brown hair and prefers to wake up late
- Denominator: Number of all items
- Conditional probability: $p(W=$ late $\mid H=$ brown $)=\frac{30}{50}$
- Probability that one of the brown-haired participants prefers to wake up late
- Denominator: Number of remaining items (after conditioned event has happened)


## Conditional and Joint Probabilities

Example

|  | brown | red | margin |
| :--- | ---: | ---: | ---: |
| early | $p(W=e, H=b)=0.31$ | $p(W=e, H=r)=0.15$ | $p(W=e)=0.46$ |
| late | $p(W=l, H=b)=0.46$ | $p(W=l, H=r)=0.08$ | $p(W=l)=0.54$ |
| margin | $p(H=b)=0.77$ | $p(H=r)=0.23$ | $p(\Omega)=1$ |

Table: (Joint) Probabilities, derived by dividing everything by $|\Omega|$

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p(A \mid B)=\frac{p(A, B)}{p(B)} \quad \text { definition of conditional probabilities }
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p(W=\text { late } \mid H=\text { brown }) & =\frac{30}{50}=0.6 \quad \text { intuition from previous slide }
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&=\frac{p(W=\text { late, } H=\text { brown })}{p(H=\text { brown })} \text { by applying definition } \\
&=\frac{0.46}{0.77}=0.6 \\
& \text { Session } 2
\end{aligned}
$$

Section 2

Collocations

## Introduction

A collocation is an expression consisting of two or more words that correspond to some conventional way of saying things.
(Manning/Schütze, 1999, 151)

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## Examples

- »Das ist mein zweites Frühstück" (adjective noun)
- „Da müssen wir Abhilfe schaffen " (noun verb)
- „Es regnet in Strömen" (verb preposition noun)


## Limited Compositionality

- Compositionality: The meaning of linguistic expressions can be understood from understanding their parts
- Collocations: Not entirely true
- I.e., they are learned by heart and stored in lexicon


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- Compositionality: The meaning of linguistic expressions can be understood from understanding their parts
- Collocations: Not entirely true
- I.e., they are learned by heart and stored in lexicon
- Related concepts
- Idiomatic expressions, metaphors, figure of speech ...


## Why are Collocations Interesting?

- Generation: Produce natural sounding expressions

> E.g., »Da müssen wir Abhilfe schaffen« instead of »Da müssen wir Abhilfe erzeugen «

- Parsing: Collocations are more likely to also be syntactic phrases
- Lexicography: Collocations should be included in dictionaries
- Social justice: Collocations may be important in reinforcing cultural stereotypes


# How to Detect Collocations Quantitatively? 

Multiple methods

- Frequency
- (Pointwise) Mutual Information

Subsection 1
Frequency

## Counting Bigrams

- Simple idea: We count bigrams (i.e., pairs of subsequent tokens)


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- Corpus: Wikipedia pages (first 10000 sentences)

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| wurde er | 630 |
| in der | 623 |
| wurde die | 501 |
| an der | 386 |
| mit dem | 363 |
| in die | 362 |
| in den | 329 |
| mit der | 312 |
| wurde das | 291 |
| wurde der | 291 |
| für die | 248 |
| er in | 193 |
| war er | 181 |
| von der | 174 |
| wo er | 169 |
| bei den | 168 |
| bei der | 166 |
| und wurde | 165 |
| an die | 161 |
| und die | 150 |
| er die | 143 |
| er als | 142 |
| er mit | 142 |
| wurden die | 142 |
| auf dem | 135 |
| für den | 133 |
| wurde sie | 127 |
| er zum |  |
| auf der | 123 |
| $122^{1 / 31}$ |  |

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- Again, there are a lot of function words. Why?

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| er die | 143 |
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- Corpus: Wikipedia pages (first 10000 sentences)
- Again, there are a lot of function words. Why?
- Zipf's law: Two words that are highly frequent have much higher chance to co-occur with high frequency

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## Counting Bigrams

- Content words: Nouns, verbs, adjectives, adverb
- My operationalization here: Remove everything that doesn't contain one upper-case letter
- Because verb-verb combinations are rare (as bigrams)
- But we're missing verb-adverb combinations


## Counting Bigrams

Content Words

| Bigram | Frequency |
| :--- | ---: |
| Jahre alt | 56 |
| Bevölkerung waren | 47 |
| Prozent waren | 46 |
| Jahre später |  |
| of Fame | 45 |
| Hall of | 44 |
| New York | 43 |
| als Nachfolger | 41 |
| Olympischen Spielen | 41 |
| Professor für |  |
| ersten Mal | 35 |
| er Mitglied | 32 |
| Fame aufgenommen | 32 |
| selben Jahr | 29 |
| Zweiten Weltkrieg | 28 |
| zum Mitglied | 28 |
| zum Professor | 26 |
| Jahr später | 25 |
| zwei Jahre | 24 |
| University of | 23 |
| Professor an | 22 |
| nach Deutschland | 21 |
| Betrieb genommen | 20 |
| Bevölkerung war | 20 |
| Los Angeles | 18 |
| drei Jahre | 18 |
| als Professor | 18 |
| Im Jahr |  |
| Lehrstuhl für | 18 |

## Focus Words

- Look at bigrams that contain a specific word
- In this case: »Gründen"


## Focus Words

| Bigram | Frequency |
| :--- | ---: |
| gesundheitlichen Gründen | 7 |
| Gründen von | 3 |
| finanziellen Gründen | 2 |
| Gründen abgeben | 1 |
| Gründen als | 1 |
| Gründen auf | 1 |
| Gründen aus | 1 |
| Gründen den | 1 |
| Gründen die | 1 |
| Gründen gab | 1 |
| Gründen ihre | 1 |
| Gründen interessierte | 1 |
| Gründen nach | 1 |
| Gründen um | 1 |
| Gründen zurück | 1 |
| disziplinarischen Gründen | 1 |
| gesundheitlichen Problemen | 1 |
| nationalpolitischen Gründen | 1 |
| paläographischen Gründen | 1 |
| persönlichen Gründen | 1 |
| politischen Gründen | 1 |
| strategischen Gründen | 1 |

## Subsection 2

Point-wise Mutual Information

## Introduction

## Example

»1910 wurde Gerland $\qquad$
$\qquad$ in Jena.«

- Knowing one word makes predicting the next easier
- One word provides information about the next - it reduces insecurity


## Introduction

## Example

»1910 wurde Gerland außerordentlicher $\qquad$ in Jena. «

- Knowing one word makes predicting the next easier
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## Introduction

## Example

»1910 wurde Gerland außerordentlicher Professor in Jena."

- Knowing one word makes predicting the next easier
- One word provides information about the next - it reduces insecurity


## Intuition

- We are interested in the (potential) collocation »außerordentlicher Professor"


## Intuition

| Word | Counts | Frequency |
| :--- | ---: | :---: |
| außerordentlicher | 109 | $5.5 \times 10^{-6}$ |
| Professor | 2126 | $1 \times 10^{-4}$ |
| All | 19811129 | 1 |

- We are interested in the (potential) collocation »außerordentlicher Professor"
- We interpret relative frequencies as probabilities
- If we pick a random word, the probability that it is »Professor«, is $1 \times 10^{-4}$ : $p(W=$ Professor $)=1 \times 10^{-4} \simeq 0.00010731$


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$p(W=$ außerordentlicher $) \times p(W=$ Professor $)=5.5 \times 10^{-10}$


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- If we pick two random words, how likely is it that they are »außerordentlicher« and »Professor«?
$p(W=$ außerordentlicher $) \times p(W=$ Professor $)=5.5 \times 10^{-10}$
- This is the probability that these two words appear together - if they are distributed randomly / independent events

Pointwise Mutual Information

$$
\operatorname{pmi}\left(w_{1}, w_{2}\right)=
$$

## Pointwise Mutual Information

$$
\operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} \overline{p\left(W=w_{1}\right) p\left(W=w_{2}\right)}
$$

- Denominator: Probability that the words appear together, if they are distributed randomly


## Pointwise Mutual Information

$$
\operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} \frac{p\left(B=\left\langle w_{1}, w_{2}\right\rangle\right)}{p\left(W=w_{1}\right) p\left(W=w_{2}\right)}
$$

- Denominator: Probability that the words appear together, if they are distributed randomly
- Numerator: Probability that they actually appear together


## Pointwise Mutual Information

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- Denominator: Probability that the words appear together, if they are distributed randomly
- Numerator: Probability that they actually appear together
- $\log _{2}$ : Scales


## Interpretations

$$
\operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} \frac{p\left(w_{1}, w_{2}\right)}{p\left(w_{1}\right) p\left(w_{2}\right)}
$$

- Fraction between real and expected co-occurrence probability


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\operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} \frac{p\left(w_{1}, w_{2}\right)}{p\left(w_{1}\right) p\left(w_{2}\right)}
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- Fraction between real and expected co-occurrence probability
- Thought experiments
- No dependence - co-occurrence has same probability as by chance
- $p\left(w_{1}\right)=0.01, p\left(w_{2}\right)=0.01, p\left(w_{1}, w_{2}\right)=0.0001, \Rightarrow \operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} 1=0$


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- Co-occurrence is 8 times more probable than by chance
- $p\left(w_{1}\right)=0.01, p\left(w_{2}\right)=0.01, p\left(w_{1}, w_{2}\right)=0.008, \Rightarrow \operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} \frac{0.0008}{0.0001}=3$


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$$
\operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} \frac{p\left(w_{1}, w_{2}\right)}{p\left(w_{1}\right) p\left(w_{2}\right)}
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- Co-occurrence is 8 times less probable than by chance
- $p\left(w_{1}\right)=0.01, p\left(w_{2}\right)=0.01, p\left(w_{1}, w_{2}\right)=0.0000125, \Rightarrow \operatorname{pmi}\left(w_{1}, w_{2}\right)=\log _{2} \frac{0.0000125}{0.0001}=-3$

Section 3

Summary

## Summary

- Probability theory
- Probability: Ratio of events of interest to all possible events (within event space)
- Joint probability: Two events take place simultaneously
- Conditional probability: One event takes place under the assumption that another event took place
- Dependent and independent events
- Collocations
- Multiple words that have a meaning beyond their parts (non-compositionality)
- Counting n-grams: Function word combinations are most frequent
- Pointwise Mutual information: Metric how much information one word yields about another


## References I

囲 Manning, Christopher D./Hinrich Schütze (1999). Foundations of Statistical Natural Language Processing. Cambridge, Massachusetts and London, England: MIT Press.

