

- Evaluation of machine learning models
- Accuracy, error rate
 - Single score for entire classification
- Precision, Recall, F-Score
 - Scores for each class
 - ▶ Precision: How many of the items classified as *c* are truly category *c*?
 - Recall: How many of the items that are truly c did the system find?
- Baseline

Das Data Center for the Humanities (DCH) an der Universität zu Köln sucht zum nächstmöglichen Zeitpunkt eine Studentische Hilfskraft (w/m/d) (für bis zu 24 Monate, 19 Stunden/Woche)

Das Data Center for the Humanities (DCH) berät und unterstützt als geisteswissenschaftliches Datenzentrum an der Universität zu Kolin Forschende der Philosophischen Fakultät im Bereich Forschungsdatenmanagement. Zur Unterstützung im Bereich Öffentlichkeitsarbeit, Veranstaltungsorganisation und Kommunikation sucht das DCH zum nächstmöglichen Zeitpunkt eine wissenschaftliche Hilfsfaraft (WHB).

Aufgaben

- Unterstützung und Zuarbeit innerhalb fachwissenschaftlicher und technischer Recherche
- Unterstützung bei der Organisation von internen und öffentlichen Workshops und Vernetzungsveranstaltungen
- Redaktionelle Arbeiten und Layout des Jahresberichts des DCH
- Design von wissenschaftlichen Postern und Awareness-Materialien im Forschungsdatenmanagement
- Unterstützung des DCH-Teams bei der technischen und inhaltlichen Betreuung von Websites

Notwendige Kenntnisse und Kompetenzen

- Geisteswissenschaftliches Studium, idealerweise mit starkem Forschungsschwerpunkt
- gute/sehr gute Deutsch- und Englischkenntnisse

Wünschenswerte Kenntnisse und Kompetenzen

- Interesse an Content Management Systemen (Typo3, Wordpress)
- Adobe InDesign- und Illustrator-Kenntnisse
- Erfahrung im Umgang mit digitalen Daten
- · Erfahrung bei der Abfassung von wissenschaftlichen Texten

- Verständnis für Strukturen an Hochschulen
- Selbstsicherer Umgang mit Forscher:innen verschiedener Disziplinen

Bewerbungsfinst: 31.05.2024 Bewerbungen mit Lebenslauf sind elektronisch einzureichen bei patrick-helling@unikoein.de





$\begin{array}{l} \mbox{Decision Tree} \\ \mbox{Sprachverarbeitung (VL + \ddot{U})} \end{array}$

Nils Reiter

May 16, 2024







What are the instances?



- What are the instances?
 - Situations we are in (this is not really automatisable)



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 - Situations we are in (this is not really automatisable)
- What are the features?



- What are the instances?
 - Situations we are in (this is not really automatisable)
- What are the features?
 - Consciousness
 - Clothing situation
 - Promises made

...

Whether we are driving

► Well-established data structure in CS

Trees



- Well-established data structure in CS
- A tree is a pair that contains
 - some value and
 - a (possibly empty) set of children
 - Children are also trees

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Prediction Model



- Each non-leaf node in the tree represents one feature
- Each leaf node represents a class label
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 - Number of branches = $|v(f_i)|$ (number of possible values)



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- Each leaf node represents a class label
- Each branch at this node represents one possible feature value
 - Number of branches = $|v(f_i)|$ (number of possible values)
- Make a prediction for *x*:
 - 1. Start at root node
 - 2. If it's a leaf node
 - assign the class label
 - 3. Else
 - Check node which feature is to be tested (f_i)
 - Extract $f_i(x)$
 - Follow corresponding branch
 - Go to 2





Core idea: The tree represents splits of the training data

- 1. Start with the full data set D_{train} as D
- 2. If D only contains members of a single class:

Done.

- 3. Else:
 - Select a feature f_i
 - Extract feature values of all instances in D
 - Split the data set according to f_i : $D = D_a \cup D_b \cup D_c \dots$ $D_{\alpha} = \{x \in D | f_i(x) = \alpha\}, a, b, c \in v(f_i)$
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Remaining question: How to select features?

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 - Increase
 {♠♠♠♡} = {♡} ∪ {♠♠♠} ← better split!
 No increase
 - $\{ \bigstar \spadesuit \spadesuit \heartsuit \} = \{ \diamondsuit \} \cup \{ \clubsuit \spadesuit \heartsuit \}$
- Homogeneity: Entropy/information

Shannon (1948)

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Shannon (1948)

- Rule: Always select the feature with the highest information gain (IG)
 - (= the highest reduction in entropy = the highest increase in homogeneity)



- Measures the amount of uncertainty
- How uncertain is the next symbol in these sequences?
 - ▶ aaaaaaaaaaaaaaaaaaa



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 - nmkfjigeahldcb 14 symbols, very uncertain
- Certainty depends on number of different symbols and on their distribution

$$H(X) = -\sum_{i=1}^{n} p(x_i) \log_b p(x_i)$$

 $Casing = \{ T, b, - \}$ STALL-5 entropy of random variable X $\int \int \int \frac{1}{H(X)} = \bigcap \sum_{i=1}^{n} p(x_i) \log_b p(x_i)$





entropy of random variable X

$$\int_{n}^{n} \int_{n}^{n \text{ relative frequency of the class}} \log_{b}(x) = y$$

$$H(X) = -\sum_{i=1}^{n} p(x_{i}) \log_{b} p(x_{i})$$

$$\log_{b}(x) = y$$

$$\exp(x_{i}) \log_{b} y(x_{i})$$

$$e^{2x} + 2x$$

Interpretation

Entropy is the average number of bits^{*} we need to specify an outcome of the random variable (* for b = 2)

Entropy (Shannon, 1948) Examples



Entropy (Shannon, 1948) Examples

$$\begin{split} H(\{ \bigstar \bigstar \bigstar \}) &= -\frac{4}{4} \log_2 \frac{4}{4} = 0 \\ H(\{ \bigstar \bigstar \bigstar \}) &= -\left(\underbrace{\frac{3}{4} \log_2 \frac{3}{4}}_{\bigstar} + \underbrace{\frac{1}{4} \log_2 \frac{1}{4}}_{\heartsuit} \right) = 0.811 \\ H(\{ \bigstar \bigstar \heartsuit \heartsuit \}) &= \ldots = 1 = H(\{ \bigstar \bigstar \circlearrowright \heartsuit \heartsuit \diamondsuit \}) = \ldots \\ H(\{ \bigstar \circlearrowright \heartsuit \clubsuit \rbrace) &= 1.585 \\ H(\{ \bigstar \heartsuit \clubsuit \diamondsuit \}) &= (2) \\ H(\{ \underline{nmkfjigeahldcb}\}) &= 3.807 \end{split}$$

Entropy Mutual Information

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 - Joint entropy: Amount of uncertainty in two random variables
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 - $MI(X, Y) = H(X) H(X|Y) = H(Y) H(Y|X) = \sum_{x,y} p(x,y) \log_2 \frac{p(x,y)}{p(x)p(y)}$

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- Point-wise Mutual Information
 - Statement about values of random variable (i.e., occurrence of specific word)

•
$$I(w_1, w_2) = \log_2 \frac{p(w_1, w_2)}{p(w_1)p(w_2)}$$

Manning/Schütze, 1999, 67

$$H(\{ \clubsuit \clubsuit \heartsuit \}) = H([3,1]) = 0.562$$
$$H(\{ \heartsuit \}) = H([1]) = 0$$
$$H(\{ \clubsuit \clubsuit \}) = H([3]) = 0$$

$$\begin{array}{rl} & \begin{array}{c} & \begin{array}{c} & \begin{array}{c} & \begin{array}{c} & \begin{array}{c} \\ & \left\{ \bigstar \bigstar \heartsuit \heartsuit \right\} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ & \end{array} \\ \\ & \end{array} \\ & \end{array} \\ & \begin{array}{c} \\ & \end{array} \\ & \end{array} \\ \\ \\ \end{array} \\ \\ \\ \end{array} \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \end{array} \\ \\ \\ \end{array} \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \\ \\ \end{array} \\ \\$$

 $\begin{array}{rcl} H(\{ \bigstar \bigstar \diamondsuit \circlearrowright \}) &=& H([3,1]) = 0.562 \\ H(\{ \heartsuit \}) &=& H([1]) = 0 \\ H(\{ \diamondsuit \bigstar \bigstar \}) &=& H([3]) = 0 \end{array} \qquad \begin{array}{rcl} H(\{ \bigstar \bigstar \circlearrowright \And) &=& H([3,1]) = 0.562 \\ H(\{ \diamondsuit \bigstar \circlearrowright) &=& H([1]) = 0 \\ H(\{ \diamondsuit \bigstar \circlearrowright \}) &=& H([1]) = 0 \\ H(\{ \diamondsuit \bigstar \circlearrowright \}) &=& H([2,1]) = 0.637 \end{array}$

$$\begin{array}{rcl}
\widehat{IG}(f_1) &= & \widehat{H(\{ \clubsuit \clubsuit \heartsuit \heartsuit \})} \underbrace{\operatorname{avg}_{\operatorname{micro}}(H(\{ \heartsuit \}), H(\{ \clubsuit \clubsuit \clubsuit \}))} \\
&= & 0.562 - 0 = \underline{0.562} \\
IG(f_2) &= & H(\{ \clubsuit \clubsuit \clubsuit \heartsuit \}) - \operatorname{avg}_{\operatorname{micro}}(H(\{ \clubsuit \}), H(\{ \clubsuit \clubsuit \heartsuit \})) \\
&= & 0.562 - (\frac{3}{4}0.637 + \frac{1}{4}0) \\
&= & 0.562 - 0.562 - 0.477 = \underline{0.085}
\end{array}$$

Feature Selection using Entropy

- We calculate entropy for the target class
- But in different sub sets of the data set

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Listing 2: Feature selection in pseudo code for a data set D

```
function select feature(D):
    base_entropy = entropy(D)
2
    ig map = \{\}
3
    foreach feature f:
4
      weighted_feature_entropy = 0
5
6
     foreach feature value v:
7
        D_v = subset of D with all instances that have the value v
8
        sub entropy = entropy(D v)
        sub_size = length(D_v)
9
        weighted_feature_entropy = weighted_feature_entropy + ( sub_entropy * sub_size )
10
      information gain = base entropy - ( (weighted feature entropy) / length(D) )
11
      ig_map.put(f, information_gain)
12
    return maximum from ig_map
13
```

J. Ross Quinlan (1986). »Induction of Decision Trees«. In: *Machine Learning* 1.1, pp. 81–106. DOI: 10.1007/BF00116251

Limitations

- Only categorical attributes
- Cannot handle missing values
- Tends to overfit: »In my experience, almost all decision trees can benefit from simplification« (Quinlan, 1993, 36)
 - Even today, overfitting is a huge challenge for ML algorithms!

 \Rightarrow Extension: C4.5

(Quinlan, 1993)





Subsection 1

Example: Spam Classification

Data set

b Data set: 100 e-mails, manually classified as spam or not span (50/50)

- Classes $C = \{\underline{\text{true}}/1, \underline{\text{false}}/0\}$
- Features: Presence of each of these tokens (manually selected): >casino<, >enlargement<, >meeting<, >profit<, >super<, >text<, >xxx

Mail	casinor)enlargement()	meeting	profit	super	itexti)XXX(С
1	1	1	0	0	Ô	1	1	0
2	0	1	0	1	70	0	0	1
3	1	0	1	0	$\overset{\mathbf{U}}{1}$	0	0	0
4	1	1	1	0	0	0	0	0
5	0	1	1	0	0	1	1	1
	•						•	•

First step: Use the full data set

H(full data set) = 1

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 $\begin{array}{rcl} H(\mbox{full data set}) &=& 1\\ H(\mbox{scaino}(=1)) &=& 0.9991\\ H(\mbox{scaino}(=0)) &=& 0.9985 \end{array}$



First step: Use the full data set

$$\begin{array}{rcl} H(\text{full data set}) &=& 1\\ H(\text{pcasino}(=1)) &=& 0.9991\\ \hline H(\text{pcasino}(=0)) &=& 0.9985\\ \hline H(\text{pcasino}) &=& \frac{(56 \times 0.9991) + (44 \times 0.9985)}{100} \textcircled{0.9989}\\ \hline IG(\text{pcasino}) &=& 1 - 0.9989 \swarrow 0.0012\\ \hline IG(\text{profit}) &=& 0.0073\\ \vdots & \vdots \end{array}$$

First step: Use the full data set



$$\begin{array}{rcl} H(\mbox{full data set}) &=& 1\\ H(\mbox{λcasinα} \in 1) &=& 0.9991\\ H(\mbox{λcasinα} \in 0) &=& 0.9985\\ H(\mbox{λcasinα}) &=& \frac{(56 \times 0.9991) + (44 \times 0.9985)}{100} = 0.9989\\ IG(\mbox{λcasinα}) &=& 1 - 0.9989 = 0.0012\\ IG(\mbox{λprofit$}) &=& 0.0073\\ \vdots & \vdots \end{array}$$

Next step: Use the data set *after* application of the first selected feature profit = 0

 $\begin{array}{rcl} H({\rm data \ set}) &= & 0.99403 \\ H({\rm b}{\rm casino}\,(=1) &= & 0.9910 \\ H({\rm b}{\rm casino}\,(=0) &= & 0.9963 \\ IG({\rm b}{\rm casino}\,() &= & 0.00029 \\ IG({\rm b}{\rm text}\,() &= & 0.01151 \end{array}$



Next step: Use the data set *after* application of the first selected feature \Rightarrow profit (= 0 \Rightarrow profit (= 1)

$$H(\text{data set}) = 0.99403$$

 $H(\text{rcasino} \epsilon = 1) = 0.9910$
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H(data set) = 0.99107

$$H($$
 casino (= 1) = 0.9366

$$H($$
 casino $(=0) = 1$

$$IG($$
 casino() = 0.0150

 $IG(\mathsf{smeeting})$





Next step: Use the data set *after* application of the first selected feature $\Rightarrow profit = 0$ $\Rightarrow profit = 1$

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- IG(casino() = 0.0150
- IG(smeetings) = 0.00029

Next step: Use the data set after application of the first two layers of selected features



Section 1

Summary

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Decision Tree

Summary

- Prediction model
 - Transparent: Easy to apply by fumans/
 - Easy to implement: Follow the path from root to leaf
- Learning algorithm
 - Recursively split the training data set according to features
 - Use information gain to maximize the homogeneity in the sub sets
- Compared with Naive Bayes
 - Feature dependence modeled through tree structure
- ► DT in Weka: Try for yourselves! ☺

References I

- Manning, Christopher D./Hinrich Schütze (1999). *Foundations of Statistical Natural Language Processing*. Cambridge, Massachusetts and London, England: MIT Press.
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